Code No: 09A30402

## JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY, HYDERABAD B. Tech II Year I Semester Examinations, November/December-2013

Signals and Systems (Common to ECE, EIE, ETM, BME)

Time: 3 hours

Max. Marks: 75

## Answer any five questions All questions carry equal marks

X.a) Define a Signal. What are the different types of signals?

- b) Derive the expression for component vector  $C_{12}$  of approximating the function  $f_1(t)$  over  $f_2(t)$  and also prove that the component vector becomes zero if the  $f_1(t)$  and  $f_2(t)$  are orthogonal.
- Show that the following two signals are orthogonal over a interval [0 1] for  $f_1(t) = 2$  and  $f_2(t) = \sqrt{3}(1-2t)$ . [3+6+6]
- Represent the function  $e^t$  over the interval  $0 \le t \le 1$  by the trigonometric Fourier series.
  - b) Obtain the exponential Fourier series for the full wave rectified sine wave shown in Figure 1 below. [8+7]

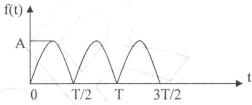


Figure 1

- 3.a) Define Fourier Transform and State any four properties.
- b) Find the Fourier transform of Signum function and double sided real function e<sup>-a|t|</sup>.

  [7+8]
- 4.a) Show that the output of an LTI system is given by the convolution sum of the input and system function
  - b) Determine whether the following systems are Linear and Time Invariant or not. i)  $y(n) = x(n^2)$  ii)  $y(n) = x^2(n)$  iii)  $y(n) = e^{x(n)}$ . [9+6
- Define Nyquist rate. Compare the merits and demerits of performing sampling using impulse, Natural and Flat-top sampling techniques.
  - b) Discuss the process of reconstructing the signal from its samples. [8+7]
- 6.a) Define Convolution Theorem in Time and Frequency domain and bring out the expression for convolution in Time domain.
  - b) Find the convolution of the signals  $x(t) = e^{-2t} u(t)$  and  $y(t) = e^{-4t} u(t)$ . [8+7]
- (a) Define Laplace Transform and discuss its existence
  - b) Find Laplace Transform of (i)  $x(t) = t^2u(t)$  (ii)  $x(t) = e^{-at} \sinh \omega t \ u(t)$ . [7+8]
- 8.a) Determine the inverse Z-Transform of  $X(z) = z/(3z^2 4z + 1)$ , if the region of convergence are (i) z > 1 (ii) z < 1/3 (iii) 1/3 < z < 1.
  - b) Using scaling property determine the Z-transform of a<sup>n</sup> cosωn and find its ROC.

[8+7]